

SYNTHESIS AND SPECTROSCOPIC CHARACTERIZATION OF LITHIUM SALTS OF COPPER(II) AND NICKEL(II) COMPLEXES WITH 1,3-PROPANEDIAMINE-*N,N,N',N'*-TETRAACETATE

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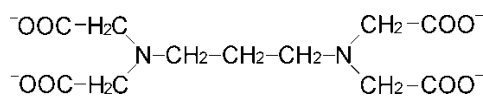
ABSTRACT

The complexes $\text{Li}_2[\text{Ni}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ and $\text{Li}_2[\text{Cu}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (where 1,3-pdta represents the 1,3-propanediaminetetraacetate anion) have been synthesized and characterized by applying IR and UV-vis spectroscopy. The obtained spectroscopic results of these complexes are discussed in relation to those for $\text{Mg}[\text{M}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ complexes ($\text{M} = \text{Ni(II)}$ and Cu(II)) of known crystal structure.

Keywords. Nickel(II) complexes, Copper(II) complexes, 1,3-pdta, IR spectroscopy, UV-vis spectrophotometry.

INTRODUCTION

The hexadentate 1,3-pdta ligand (1,3-pdta = 1,3-propanediamine-*N,N,N',N'*-tetraacetate anion) has been used for preparation of complexes with many transition metal ions (Herak et al., 1984; Rychlewska et al., 2000; Radanović et al., 2001; Radanović et al., 2003; Radanović et al., 2004; Rychlewska et al., 2005; Rychlewska et al., 2007; Rychlewska et al., 2011). In relation to edta (edta = ethylenediamine-*N,N,N',N'*-tetraacetate), the 1,3-pdta ligand has longer diamine chain and is expected to coordinate hexadentately to metal ions of various size.



1,3-pdta

The structural 1,3-pdta characteristics of the numerous hexadentate complexes of the type $\text{M}[\text{M}'(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ ($\text{M} = \text{Mg(II)}$, Co(II) , Zn(II) , Sr(II) ; $\text{M}' = \text{Cu(II)}$, Ni(II) , Co(II) , Mg(II) , Zn(II) and Sr(II)) have been determined by single-crystal X-ray diffraction analysis (Rychlewska et al., 2000; Radanović et al., 2001; Radanović et al., 2003; Radanović et al., 2004; Rychlewska et al., 2005; Rychlewska et al., 2011). Previous attempts to isolate 1,3-pdta- M(II) complexes with monovalent cations as counter ion did not give the expected results. Recently, in our laboratory by ion exchange column chromatography, $\text{Li}_2[\text{Co}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ complex was isolated (Rychlewska et al., 2008). This complex constitutes the first example of $[\text{M}(1,3\text{-pdta})]^{2-}$ complex with a monovalent cation as counter ion (Rychlewska et al., 2008). The structure of this complex consists of two tetrahedrally coordinated Li^+ cations, an octahedral $[\text{Co}(1,3\text{-pdta})]^{2-}$ anion and five water molecules, two of which are crystalline water molecules. As a continuation of our

research, in the present paper, we report synthesis and spectroscopic characterization of two new Cu(II) and Ni(II) complexes with general formula $\text{Li}_2[\text{M}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$.

EXPERIMENTAL

Materials and methods

All commercially obtained reagent-grade chemicals were used without further purification. The preparation of $\text{Ba}_2(1,3\text{-pdta})\cdot 2\text{H}_2\text{O}$ has been reported elsewhere (Radanovic et al., 2000). The IR spectra were recorded on a Perkin-Elmer Spectrum One FT-IR spectrometer using the KBr pellet technique. The UV-vis spectra of Ni(II) and Cu(II) complexes were recorded on a Perkin-Elmer spectrophotometer. The following concentrations of aqua solutions have been used for these measurements: 10^{-2} M for Ni(II) and 10^{-3} M for Cu(II) complexes. Elemental microanalysis for carbon, hydrogen and nitrogen were performed by the Microanalytical Laboratory, Department of Chemistry, Faculty of Science, University of Belgrade.

Synthesis of $\text{Li}_2[\text{Ni}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (1) and $\text{Li}_2[\text{Cu}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (2) complexes

0.01 mol of $\text{CuSO}_4\cdot 5\text{H}_2\text{O}$ (2.50 g) or $\text{NiSO}_4\cdot 7\text{H}_2\text{O}$ (2.83 g) in 60 ml of H_2O was stirred at 80°C for 10 min. To this solution, solid $\text{Ba}_2(1,3\text{-pdta})\cdot 2\text{H}_2\text{O}$ (6.13 g, 0.01 mol) was added and the obtained solution ($\text{pH} = 7$) was stirred at 80°C for 3 h. The precipitated BaSO_4 was filtered off and to the obtained filtrate, the solid $\text{MgSO}_4\cdot 6\text{H}_2\text{O}$ (2.28 g; 0.01 mol) was added and stirring with heating at 60°C was continued for the next 20 min. The precipitated BaSO_4 was again filtered off. To the obtained filtrate, 5–6 ml of ethanol was added and the solution was left to stand in a refrigerator for several days. The crystals of $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ (3.34 g, 66%) and $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ (3.38 g, 63%) were collected, washed with ethanol, then ether and air-dried.

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Anal. Calc. for $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$, $\text{MgCuC}_{11}\text{H}_{30}\text{N}_2\text{O}_{16}$ (FW = 534.21): C, 24.73; H, 5.66; N, 5.24%. Found: C, 24.84; H, 4.84; N, 5.04%.

Anal. Calc. for $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$, $\text{MgNiC}_{11}\text{H}_{30}\text{N}_2\text{O}_{16}$ (FW = 529.36): C, 24.96; H, 5.71; N, 5.29%. Found: C, 24.90; H, 5.82; N, 5.32%.

The aqueous solutions of $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ (Radanović et al., 2001) and $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ (Radanović et al., 2000) were passed through a column packed with Merck I cation exchanger in the Li^+ form. The eluates were evaporated at room temperature to a volume of 2 ml and $\text{Li}_2[\text{Ni}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (**1**) and $\text{Li}_2[\text{Cu}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (**2**) complexes were crystallized after addition of ethanol and cooling in a refrigerator for 2 days. The crystals were removed by filtration and air-dried.

Anal. Calc. for $\text{Li}_2[\text{Ni}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (**1**), $\text{Li}_2\text{NiC}_{11}\text{H}_{24}\text{N}_2\text{O}_{13}$ (FW = 464.89): C, 28.42; H, 5.20; N, 6.03%. Found: C, 28.27; H, 5.22; N 6.05%.

Anal. Calc. for $\text{Li}_2[\text{Cu}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (**2**), $\text{Li}_2\text{CuC}_{11}\text{H}_{24}\text{N}_2\text{O}_{13}$ (FW = 469.74): C, 28.13; H, 5.15; N, 5.96%. Found: C, 27.93; H, 5.16; N, 5.96%.

RESULTS AND DISCUSSION

In this work two $\text{Li}_2[\text{M}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ complexes (M = Ni(II), **1** and Cu(II), **2**) were synthesized and characterized by IR and UV-vis spectroscopy. The schematic presentation of the procedure for synthesis of **1** and **2** is presented in Figure 1. The spectroscopic results of these complexes are discussed in relation to those for $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ and $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ complexes of known crystal structure (Radanović et al., 2001; Rychlewska et al., 2000).

Comparative analysis of the spectroscopic data for 1 and 2 with those for $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ and $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ complexes of known crystal structure IR spectra

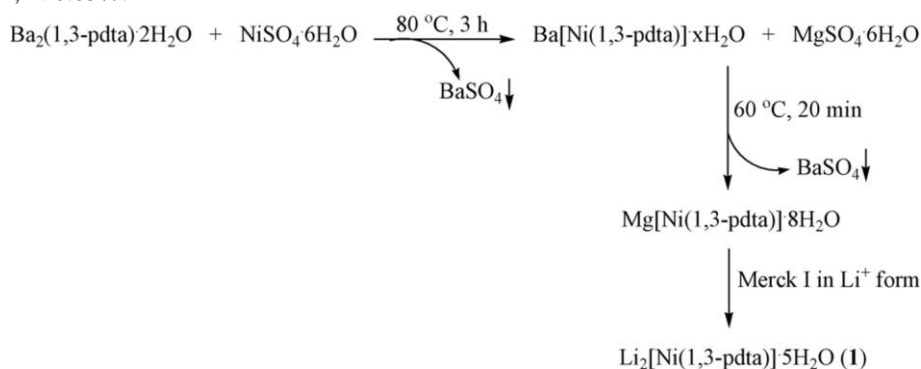


Figure 1. Schematic presentation of the procedure for the preparation of $\text{Li}_2[\text{Ni}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (**1**). The same method is used for the synthesis of $\text{Li}_2[\text{Cu}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (**2**).

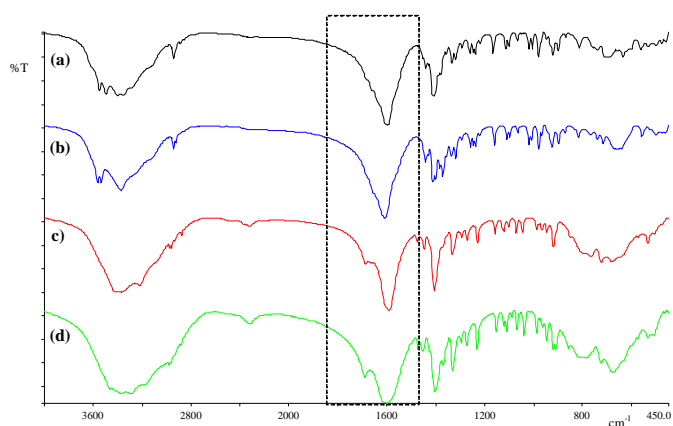


Figure 2. IR spectra of Ni(II) and Cu(II) complexes with hexadentate coordinated 1,3-pdta ligand: (a) $\text{Li}_2[\text{Ni}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (**1**), (b) $\text{Li}_2[\text{Cu}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (**2**), (c) $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ and (d) $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$.

The IR spectra of **1** and **2** are given in Figure 2. These spectra have been compared with the corresponding for $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ and $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ complexes having the same hexadentate coordinated 1,3-pdta ligand and

Mg^{2+} ion as counter cation. The crystal structures of the latter two complexes have been previously determined by single crystal X-ray diffraction analysis (Radanović et al., 2001; Rychlewska et al., 2000). The IR data of these complexes, in the region for the asymmetric carboxylate stretching frequencies, are presented in Table 1. The interpretation of these spectra was done in accordance to the previously established rule that the protonated and uncoordinated asymmetric carboxylate stretching frequencies occur at $1750 - 1700\text{ cm}^{-1}$, whereas these frequencies for the ionized and coordinated carboxylate groups are at $1650 - 1590\text{ cm}^{-1}$ (Nakamoto, 1963). As it was shown in Figure 2 and Table 1, complexes **1** and **2** in the region for the asymmetric carboxylate stretching frequencies have only one very strong and symmetric band at 1598 and 1610 cm^{-1} , respectively. This is in accordance to the fact that carboxylate groups of 1,3-pdta ligand in these two complexes are coordinated to the corresponding metal ion. Moreover, symmetric shape of these bands indicates that all glycinate rings in these complexes are equivalent. The IR spectra of **1** and **2** are very similar to those for $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ and $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ complexes. The latter two complexes in the carboxylate region

for coordinated glycinate showed very strong and broad band at 1590 and at 1599 cm^{-1} for Ni(II) and Cu(II) complexes, respectively (Table 1). Additionally, from Table 1 it can be seen that these two bands are slightly shifted to the higher energy in respect to those for complexes **1** and **2**. Moreover, the carboxylate stretching band for $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ and $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ complexes showed evidence for splitting on the higher energy side resulting in appearance of small band at 1688 for Ni(II) and 1692 cm^{-1} for Cu(II) complex.

Table 1. IR asymmetric carboxylate stretching frequencies of Ni(II) and Cu(II) complexes with 1,3-pdta ligand

Complex	$\nu_{\text{asym}} (\text{cm}^{-1})$
$\text{Li}_2[\text{Ni}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (1)	1598
$\text{Li}_2[\text{Cu}(1,3\text{-pdta})]\cdot 5\text{H}_2\text{O}$ (2)	1610
$\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$	1590; 1688(sh)
$\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$	1599; 1691(sh)

UV-vis spectra

Difference in the position and shape of the asymmetric carboxylate stretching frequencies for **1** and **2** in respect to those for $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ and $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ can be attributed to the presence of different counter cation in these two pairs of 1,3-pdta complexes. The presence of different cation in these complexes can result in their different packing in the crystal lattice as well as in different interactions between coordinated water molecules of Li^+ and Mg^{2+} counter cation and carboxylate group of $[\text{M}(1,3\text{-pdta})]^{2-}$ complex anion ($\text{M} = \text{Ni(II)}$ and Cu(II)).

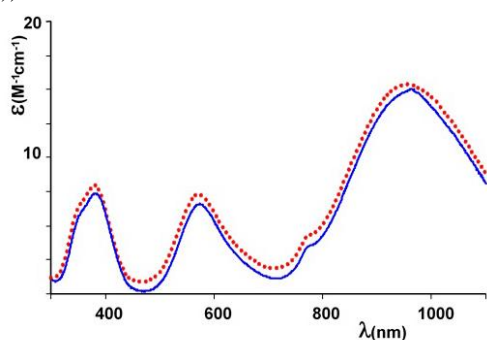


Figure 3. UV-vis spectra of **1** (···) and $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ (Radanović et al., 2001).

The UV-vis spectra of **1** and $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ complexes and their numerical data are presented in Figure 3. and Table 2. The UV-vis spectrum of $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ has been previously discussed in detail (Radanović et al., 2001), and here it has only been repeated for the sake of comparison with the spectrum of **1**. In general, it has been shown that the

spectra of Ni(II)-1,3-pdta-type complexes containing the six-membered diamine ring (**T** ring), with respect to Ni(II)-edta-type complexes with five-membered diamine ring (**E** ring), exhibit broadening of the first absorption band (D_{4h} model) (Radanović et al., 2001).

In accordance to previously established results for the Ni(II)-edta-type and most other Ni(II) complexes, the interpretation of the UV-vis spectra of **1** and $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ (Radanović et al., 2001) has been done by using an octahedral model (O_h): ${}^3A_{2g} \rightarrow {}^3T_{2g}$ (*F*) (band I); ${}^3A_{2g} \rightarrow {}^3T_{1g}$ (*F*) (band III) and ${}^3A_{2g} \rightarrow {}^3T_{1g}$ (*P*) (band IV) (Table 2). From Figure 3 it can be seen that UV-vis spectra of **1** and $\text{Mg}[\text{Ni}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ (Radanović et al., 2001) are almost identical in the shape and intensities of absorption maxima. This undoubtedly leads to the conclusion that anionic part of these two molecules are the same and represents octahedral complex containing hexadentate coordinated 1,3-pdta ligand. As it was abovementioned, the influence of counter cation on the shape and position of the carboxylate stretching frequencies was observed after measuring IR spectra of these complexes in the solid state. However, no influence of Li^+ and Mg^{2+} counter cation was observed on the shape and position of absorption maxima in the UV-vis spectra of these complexes measured in water solvent.

UV-vis spectra of **2** and $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ (Rychlewska et al., 2000) and corresponding numerical data are given in Figure 4 and Table 2. The UV-vis spectrum of $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ complex has been previously reported (Rychlewska et al., 2000) and, in the present work, it has been repeated for comparison with the spectrum of **2**. As it can be seen from Figure 4, complexes **2** and $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ have one unsymmetrical absorption band in the expected region, what is in accordance to the fact that these complexes have the same N_2O_4 donor system and C_2 molecular symmetry.

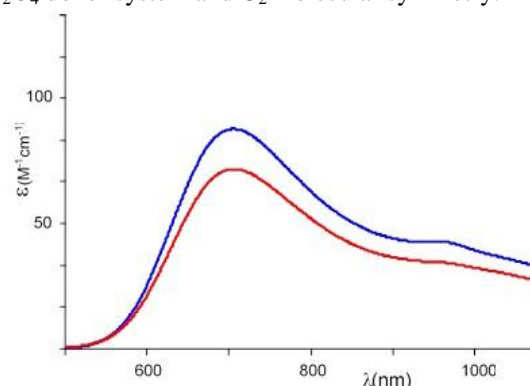


Figure 4. UV-vis spectra of **2** and $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ (Rychlewska et al., 2000).

This band can be assigned to the d_z^2 , d_{xy} , d_{xz} , $d_{yx} \rightarrow d_x^2 - d_y^2$ transitions with a $d_x^2 - d_y^2$ ground state. The UV-vis spectra of **2** and $\text{Mg}[\text{Cu}(1,3\text{-pdta})]\cdot 8\text{H}_2\text{O}$ complexes are identical in the position of the absorption maxima. However, there is small difference in the intensity of these absorption bands resulted in

the presence of different counter cation and number of water molecules in these two complexes.

Table 2. UV-vis numerical data of **1** and **2** in comparison to those for Mg[Ni(1,3-pdta)]·8H₂O (Radanović et al., 2001) and Mg[Cu(1,3-pdta)]·8H₂O (Rychlewska et al., 2000) complexes with hexadentate 1,3-pdta ligand

Complex	Absorption		Assignments <i>O_h</i>	
	λ (nm)	ϵ (M ⁻¹ cm ⁻¹)		
Mg[Ni(1,3-pdta)]·8H ₂ O	I	959.9	³ A _{2g} → ³ T _{2g} (F)	
		15.4		
	II	770.3		→ ¹ E _g (D)
	III	571.5		→ ³ T _{1g} (F)
Li ₂ [Ni(1,3-pdta)]·5H ₂ O (1)	I	962.1	→ ³ T _{1g} (P)	
		15.8		
	II	775.6		4.1
	III	573.2		7.3
Mg[Cu(1,3-pdta)]·8H ₂ O		706.0	85.0	
		705.1	86.0	
Li ₂ [Cu(1,3-pdta)]·5H ₂ O (2)				

CONCLUSION

In this paper, the new method for preparation of [Ni(1,3-pdta)]²⁻ (**1**) and [Cu(1,3-pdta)]²⁻ (**2**) complexes with Li⁺ counter cation has been presented. The hexadentate coordination of 1,3-pdta ligand in these complexes was confirmed by comparison of their IR and UV-vis spectra with those for Mg[Ni(1,3-pdta)]·8H₂O and Mg[Cu(1,3-pdta)]·8H₂O complexes of known crystal structure (Radanović et al., 2001; Rychlewska et al., 2000). The IR spectra of **1** and **2** are slightly different from those for Mg[Ni(1,3-pdta)]·8H₂O and Mg[Cu(1,3-pdta)]·8H₂O complexes, what can be attributed to the presence of different counter cation in these two pairs of 1,3-pdta complexes. On the other hand, no difference in the UV-vis spectra of these complexes was observed.

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